

Mass Flow Calculations Using Gas Dynamics Relations

Working Fluid: Air

Nomenclature

P_L = pressure in low pressure vessel

P_e = exit pressure

T_e = exit temperature

γ = C_p/C_v

M = mach number

V = Velocity

ρ_e = exit density

A_e = exit area of the nozzle

R = ideal gas constant of air

\dot{m} = mass flow rat

Governing Equations:

$$P_L = P_e \cdot \left(1 + \frac{\gamma - 1}{2} \cdot M^2 \right)^{\frac{\gamma}{\gamma - 1}}$$

$$a = \sqrt{\gamma \cdot R \cdot T}$$

$$V = M \cdot a$$

$$\rho = \frac{P}{RT}$$

$$A = \pi r^2$$

$$\dot{m}_{\text{dot}} = \rho AV$$

Variables

$$\gamma := 1.4$$

$$P_L := 104804 \text{ Pa}$$

$$P_e := 101100 \text{ Pa}$$

$$P_r := \frac{P_L}{P_e}$$

$$R_{\text{air}} := 287 \frac{\text{J}}{\text{kg} \cdot \text{K}}$$

$$T_e := 297.15 \text{ K}$$

$$D_{\text{nozzle}} := .008 \text{ m} \quad A_e := \pi \cdot \left(\frac{D_{\text{nozzle}}}{2} \right)^2$$

Calculation of mass flow rate from the low pressure vessel to atmosphere:

$$M := \sqrt{\left(\frac{P_r^{\frac{\gamma-1}{\gamma}} - 1 \right) \frac{2}{\gamma-1}}$$

$$M = 0.227$$

$$a := \sqrt{\gamma \cdot R_{\text{air}} \cdot T_e}$$

$$a = 345.536 \frac{\text{m}}{\text{s}}$$

$$V_e := M \cdot a$$

$$V_e = 78.542 \frac{\text{m}}{\text{s}}$$

$$\rho_e := \frac{P_e}{R_{\text{air}} \cdot T_e}$$

$$\rho_e = 1.185 \frac{\text{kg}}{\text{m}^3}$$

$$m_{\text{dot}} := \rho_e \cdot A_e \cdot V_e$$

$$m_{\text{dot}} = 4.68 \times 10^{-3} \frac{\text{kg}}{\text{s}}$$